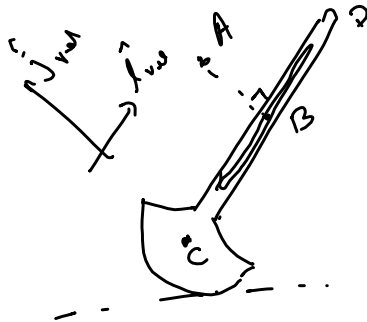


find ω_{CD} when
 $AB \perp CD$.

$$\vec{r}_{B/C} = r_{B/C} \hat{r}_{rel}$$



$$\begin{aligned} \vec{V}_B^A &= \vec{V}_A + \vec{V}_{B/A} \\ &= \vec{\omega}_{AB} \times \vec{r}_{B/A} \\ &= \omega_{AB} \hat{k} \times r_{B/A} (-\hat{j}_{rel}) \\ &= \omega_{AB} r_{B/A} \hat{i}_{rel} \end{aligned}$$

$$\begin{aligned} \vec{V}_B^C &= \vec{V}_C + \vec{V}_{B/C} \\ &= \vec{0} + \dot{r}_{rel} \hat{i}_{rel} + \vec{\omega} \times \vec{r}_{rel} \\ &= \dot{r}_{B/C} \hat{i}_{rel} + (\omega_{CD} \hat{k} \times r_{B/C} \hat{j}_{rel}) \\ &= \dot{r}_{B/C} \hat{i}_{rel} + \omega_{CD} r_{B/C} \hat{i}_{rel} \end{aligned}$$

equating velocity from A & C origins

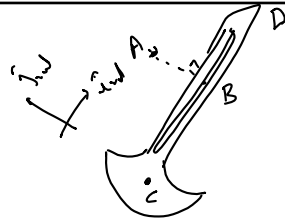
$$\vec{V}_B^A = \vec{V}_B^C$$

$$\Rightarrow \omega_{AB} r_{B/A} \hat{i}_{rel} = \dot{r}_{B/C} \hat{i}_{rel} + \omega_{CD} r_{B/C} \hat{i}_{rel}$$

$$\Rightarrow \dot{r}_{B/C} = \omega_{AB} r_{B/A}$$

$$A \quad 0 = \omega_{CD} r_{B/C}$$

$$\Rightarrow \omega_{CD} = 0$$



- calculate \vec{a}_B^c & \vec{a}_B^a
- equate \vec{a}_B^c to \vec{a}_B^a
- solve

$$\begin{aligned} \vec{a}_B^a &= \vec{a}_A + \vec{a}_{B/A} \\ &= \vec{0} + \alpha_{AB} \times \vec{r}_{B/A} + \vec{\omega}_{AB} \times (\vec{\omega}_{AB} \times \vec{r}_{B/A}) \\ &= \alpha_{AB} \times \vec{r}_{B/A} - |\vec{\omega}_{AB}|^2 \vec{r}_{B/A} \\ &= -\omega_{AB}^2 \vec{r}_{B/A} (-\hat{j}_{rel}) \\ &= \omega_{AB}^2 \vec{r}_{B/A} \hat{j}_{rel} \end{aligned}$$

$$\begin{aligned} \vec{a}_B^c &= \vec{a}_c + \vec{a}_{B/c} \\ &= \vec{0} + \ddot{r}_{rel} + 2(\vec{\omega} \times \dot{r}_{rel}) + \alpha \times \vec{r}_{rel} + \vec{\omega} \times (\vec{\omega} \times \vec{r}_{rel}) \\ &= \underbrace{\ddot{r}_{rel}}_{\text{Radial}} + \underbrace{2(\vec{\omega} \times \dot{r}_{rel})}_{\text{Coriolis}} + \underbrace{\alpha \times \vec{r}_{rel}}_{\text{Tangential}} + \underbrace{\vec{\omega} \times (\vec{\omega} \times \vec{r}_{rel})}_{\text{Centrifugal}} \\ &= \ddot{r}_{B/c} \hat{i}_{rel} + 2(\omega_{CD} \hat{k} \times \dot{r}_{B/c} \hat{i}_{rel}) + \alpha_{CD} \hat{k} \times r_{B/c} \hat{i}_{rel} + \omega_{CD} \hat{k} \times (\omega_{CD} \hat{k} \times r_{B/c} \hat{i}_{rel}) \\ &= \ddot{r}_{B/c} \hat{i}_{rel} + 2\omega_{CD} \dot{r}_{B/c} \hat{j}_{rel} + \alpha_{CD} r_{B/c} \hat{j}_{rel} - \omega_{CD}^2 r_{B/c} \hat{i}_{rel} \\ &= (\ddot{r}_{B/c} - \omega_{CD}^2 r_{B/c}) \hat{i}_{rel} + (2\omega_{CD} \dot{r}_{B/c} + \alpha_{CD} r_{B/c}) \hat{j}_{rel} \end{aligned}$$

$$\omega_{CD} = 0 \Rightarrow \vec{a}_B^c = \ddot{r}_{B/c} \hat{i}_{rel} + \alpha_{CD} r_{B/c} \hat{j}_{rel}$$

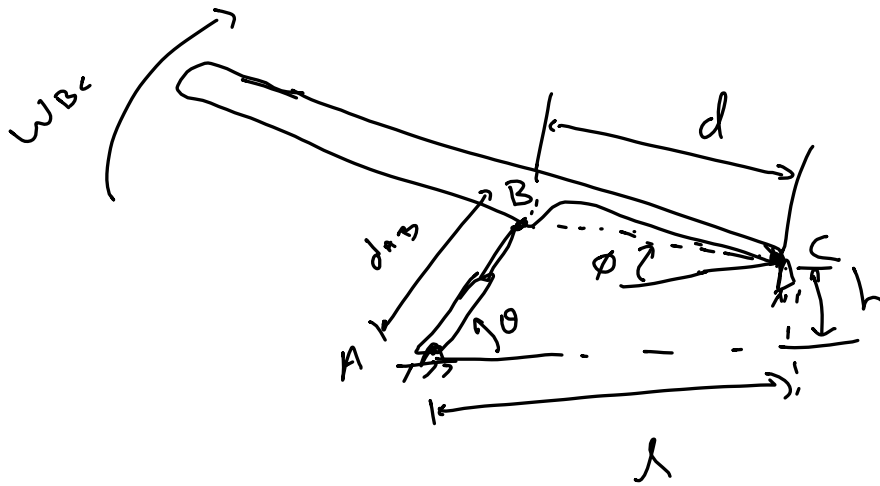
$$\vec{a}_B^a = \omega_{AB}^2 r_{B/A} \hat{j}_{rel}$$

equating \hat{i} & \hat{j} components

$$\ddot{r}_{B/c} = 0$$

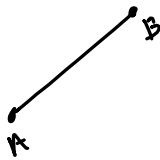
$$\alpha_{CD} r_{B/c} = \omega_{AB}^2 r_{B/A}$$

$$\Rightarrow \alpha_{CD} = \frac{\omega_{AB}^2 r_{B/A}}{r_{B/c}}$$



find \dot{d}_{A3} when $\phi = 0$, \dot{d}_{A3}

1) No arrow for vectors



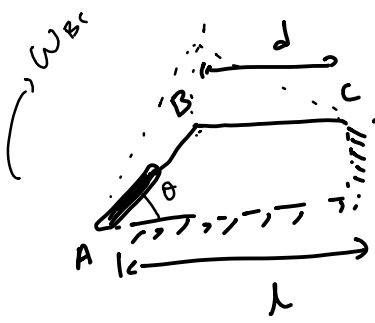
$$\vec{r}_B = \vec{r}_A + \vec{r}_{B/A} \quad | \quad \dot{r}_B = \dot{r}_A + \dot{r}_{B/A}$$

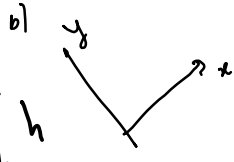
$$\vec{v}_B = \vec{v}_A + \vec{v}_{B/A}$$

$$= \vec{v}_A + \dot{r}_{B/A} \hat{u}_{r_{B/A}} + \vec{\omega} \times \vec{r}_{B/A}$$

2) Not drawing axis

3) Not drawing simplified scenario.

a) 

b) 

$$\vec{V}_B^c = \vec{V}_c + \vec{V}_{B|c}$$

$$= \vec{0} + \hat{r}_{B|c}^0 \hat{\omega}_{BC} + \vec{\omega}_{BC} \times \vec{r}_{B|c}$$

$$= \vec{\omega}_{BC} \times \vec{r}_{B|c}$$

$$= (-\omega_{BC} \hat{k}) \times (-d \cos \theta \hat{i} + d \sin \theta \hat{j})$$

$$= (-\omega_{BC} \hat{k}) \times (-d \cos \theta \hat{i})$$

$$+ (-\omega_{BC} \hat{k}) \times (d \sin \theta \hat{j})$$

$$= \omega_{BC} d \cos \theta (\hat{k} \times \hat{i}) - \omega_{BC} d \sin \theta (\hat{k} \times \hat{j})$$

$$= \omega_{BC} d \cos \theta \hat{j} + \omega_{BC} d \sin \theta \hat{i}$$

$$\vec{V}_B^c = \omega_{BC} d \sin \theta \hat{i} + \omega_{BC} d \cos \theta \hat{j}$$



$$\begin{aligned} \vec{v}_B^A &= \vec{v}_A + \vec{v}_{B/A} \\ &= \vec{0} + \dot{r}_{B/A} \hat{u}_{r_{B/A}} + \vec{\omega}_{AB} \times \vec{r}_{B/A} \\ &= \vec{0} + \dot{r}_{B/A, \text{rel}} + \vec{\omega}_{AB} \times \vec{r}_{B/A, \text{rel}} \end{aligned}$$

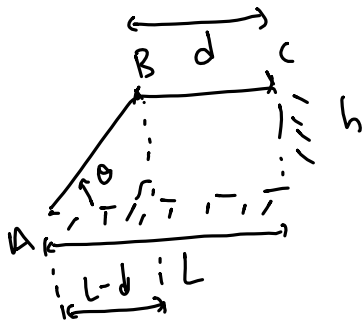
$$\begin{aligned} \vec{v}_B^A &= \dot{r}_{B/A} \hat{u}_{B/A} + \vec{\omega}_{AB} \times \vec{r}_{B/A} \\ &= \dot{d}_{AB} \hat{i} + (\omega_{AB} \hat{k}) \times (d_{AB} \hat{j}) \end{aligned}$$

$$\vec{v}_B^A = \dot{d}_{AB} \hat{i} + \omega_{AB} d_{AB} \hat{j}$$

$$\vec{v}_B^C = \omega_{BC} d \sin \theta \hat{i} + \omega_{BC} d \cos \theta \hat{j}$$

$$\dot{d}_{AB} = \omega_{BC} d \sin \theta$$

$$\omega_{AB} = \frac{\omega_{BC} d \cos \theta}{d_{AB}}$$



$$\tan \theta = \frac{h}{L-d}, \quad \cos \theta = \frac{L-d}{\sqrt{h^2 + (L-d)^2}}$$

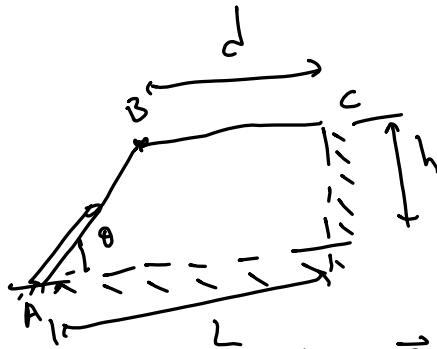
$$\sin \theta = \frac{h}{\sqrt{h^2 + (L-d)^2}}, \quad d_{AB} = \sqrt{h^2 + (L-d)^2}$$

$$\dot{d}_{AB} = \omega_{BC} d \sin \theta$$

$$\dot{d}_{AB} = \frac{\omega_{BC} d h}{\sqrt{h^2 + (L-d)^2}}$$

$$\omega_{AB} = \frac{\omega_{BC} d \cos \theta}{d_{AB}} = \frac{\omega_{BC} d (L-d)}{h^2 + (L-d)^2} //$$

$$\ddot{d}_{AB}, \quad \omega_{AB} = \frac{\omega_{BC} d (L-d)}{h^2 + (L-d)^2}$$



$$\vec{a}_B^c$$

$$\vec{a}_B$$

$$\begin{aligned} \vec{a}_B^c &= \vec{a}_c + \vec{a}_{B/c} \\ &= \vec{0} + \ddot{r}_{B/c} \hat{u}_{r_{B/c}} + \ddot{\alpha}_{BC} \times \vec{r}_{B/c} \\ &\quad + \vec{\omega}_{BC} \times (\vec{\omega}_{BC} \times \vec{r}_{B/c}) \\ &\quad + 2\dot{\gamma}_{B/c} (\vec{\omega}_{BC} \times \hat{u}_{r_{B/c}}) \end{aligned}$$

As $r_{B/c}$ is constant,

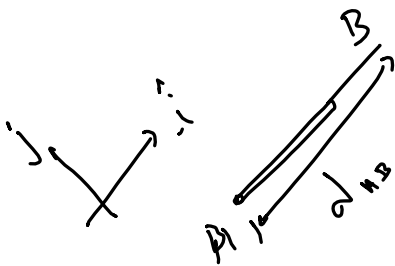
$$\vec{a}_B^c = \ddot{\alpha}_{BC} \times \vec{r}_{B/c} + \vec{\omega}_{BC} \times (\vec{\omega}_{BC} \times \vec{r}_{B/c})$$

As $\alpha_{BC} = 0$,

$$\vec{a}_B^c = \vec{\omega}_{BC} \times (\vec{\omega}_{BC} \times \vec{r}_{B/c})$$

As $\vec{\omega}_{BC} \perp \vec{r}_{B/c}$,

$$\begin{aligned} \vec{a}_B^c &= -|\vec{\omega}_{BC}|^2 \vec{r}_{B/c} \\ &= -\omega_{BC}^2 \vec{r}_{B/c} \end{aligned}$$



$$\vec{a}_B^A = \ddot{r}_{B/A} \hat{u}_{B/A} + \alpha_{AB} \times \vec{r}_{B/A} + \vec{\omega}_{AB} \times (\vec{\omega}_{AB} \times \vec{r}_{B/A}) + 2 \dot{r}_{B/A} (\vec{\omega}_{AB} \times \hat{u}_{B/A})$$

$$\begin{aligned} \vec{a}_B^A &= \ddot{d}_{AB} \hat{i} + (\alpha_{AB} \hat{k} \times d_{AB} \hat{i}) \\ &\quad - \omega_{AB}^2 (d_{AB} \hat{i}) + 2 \dot{d}_{AB} (\omega_{AB} \hat{k} \times \hat{i}) \\ &= (\ddot{d}_{AB} - \omega_{AB}^2 d_{AB}) \hat{i} + (\alpha_{AB} d_{AB} + 2 \dot{d}_{AB} \omega_{AB}) \hat{j} \end{aligned}$$

$$\begin{aligned} \vec{a}_B^C &= -\omega_{BC}^2 \vec{r}_{B/C} \\ &= -\omega_{BC}^2 (-d \cos \theta \hat{i} + d \sin \theta \hat{j}) \end{aligned}$$

Equating \hat{i} components

$$\ddot{d}_{AB} - \omega_{AB}^2 d_{AB} = \omega_{BC}^2 d \cos \theta$$

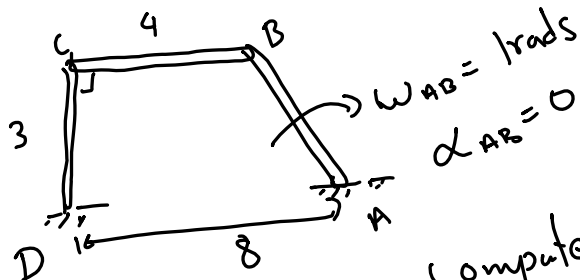
$$\ddot{d}_{AB} = \omega_{BC}^2 d \cos \theta + \omega_{AB}^2 d_{AB}$$

$$= \frac{\omega_{BC}^2 d (L-d)}{\sqrt{h^2 + (L-d)^2}} + \left(\frac{\omega_{BC} d (L-d)}{h^2 + (L-d)^2} \right)^2 \sqrt{h^2 + (L-d)^2}$$

$$= \frac{\omega_{BC}^2 d (L-d)}{\sqrt{h^2 + (L-d)^2}} \left[1 + \frac{d(L-d)}{h^2 + (L-d)^2} \right]$$

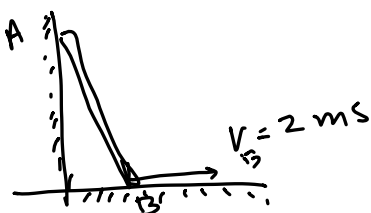
IL.

1)



compute \vec{v}_C , \vec{a}_C , α_{BC} , ω_{BC}

2)



calculate, \vec{v}_A , ω_{AB} , α_{AB}
 \vec{a}_A